An index for safety management of road networks

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- Introduction
 - Evolution of the safety management in USA
 - Current issues



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- Proposed methodology
 - Model Specification
 - Efficient Bayesian estimation



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 - Data description
 - Model results
 - Potential application



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- Conclusions & Future work



Safety Statistics

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About **35,000** fatalities and **1.7 million** injuries are annually reported in highway crashes (2005-10) across USA.

Cost of traffic crashes is reportedly more than **two and one-half times** the cost of congestion in urban areas.



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1991: Intermodal Surface Transportation Efficiency Act

— Individual states required to develop a Safety Management Systems

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- **2005:** Safe, Accountable, Flexible, Efficient Transportation Equity Act
- Establishment of Highway Safety Improvement Program (HSIP).
- 2012: Moving Ahead for Progress (MAP-21) Act
- Dramatically increased the size of HSIP program with an average annual funding of \$ 2.4 billion.
- **HSIP's data-driven strategic approach** to improve highway safety emphasizes
 - Need for comprehensive database management systems
 - state-of-the-art data analysis methodologies



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Goal: To propose

- Computationally efficient Bayesian estimation algorithm
- Safety index for road networks



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Intrinsic CAR prior:
$$\phi_i | \phi_{-i} \sim N\left(\sum_j \frac{w_{ij}}{w_{i+}} \phi_j, \frac{\tau_c^2}{w_{i+}}\right)$$



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$$\beta \sim N(b_0, B_0)$$
; $V_{\beta} \sim Wishart(\nu, V_0)$; $1/\tau_c \sim Ga(c_0, d_0)$

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NOTE: $L \& \omega$ are augmented variables.



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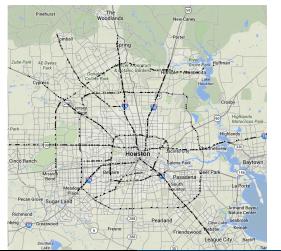
- Stationarity attainment in less than 5 minutes, which is significantly faster than existing Metropolis-Hastings based algorithms.
- Parameter estimation accuracy is more than 85%.



Empirical example

Data description

Crash data 10 different routes within Harris county, Texas. Also, included the exposure (traffic) levels in the model.

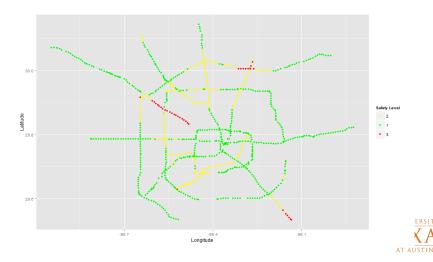




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Potential Application

Posterior means of the proposed safety index or $E(y_i|X_i)$:



Conclusions

Findings

- Framework for extracting useful information from the crash databases and to annually update the crash estimates by accumulating on the prior knowledge.
- Proposed data augmentation scheme enhances the accessibility of the sophisticated Bayesian statistical methods
- Empirical findings:
 Roads with smoother ride, higher skid resistance and minor surface distresses are generally associated with the lower crash frequencies.



Conclusions Future Work

- Incorporating the probability of ensuring a particular threshold for safety index into the project prioritization applications.
- Current model can be extended to incorporate temporal correlation of the crash counts and correlation across crash severity categories.
- The proposed safety index can be formulated as a economically weighted combination of predicted crash counts of multiple severity levels on a given road segment at any given time.



Thank You

Questions?

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